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RESEARCH ARTICLE

Information integration and collective motility in phototactic cyanobacteria

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Abstract

Cells in microbial colonies integrate information across multiple spatial and temporal scales while sensing environmental cues. A number of photosynthetic cyanobacteria respond in a directional manner to incident light, resulting in the phototaxis of individual cells. Colonies of such bacteria exhibit large-scale changes in morphology, arising from cell-cell interactions, during phototaxis. These interactions occur through type IV pili-mediated physical contacts between cells, as well as through the secretion of complex polysaccharides ('slime') that facilitates cell motion. Here, we describe a computational model for such collective behaviour in colonies of the cyanobacterium Synechocystis. The model is designed to replicate observations from recent experiments on the emergent response of the colonies to varied light regimes. It predicts the complex colony morphologies that arise as a result. We ask if changes in colony morphology during phototaxis can be used to infer if cells integrate information from multiple light sources simultaneously, or respond to these light sources separately at each instant of time. We find that these two scenarios cannot be distinguished from the shapes of colonies alone. However, we show that tracking the trajectories of individual cyanobacteria provides a way of determining their mode of response. Our model allows us to address the emergent nature of this class of collective bacterial motion, linking individual cell response to the dynamics of colony shape.

Author summary

Microbial colonies in the wild often consist of large groups of heterogeneous cells that coordinate and integrate information across multiple spatio-temporal scales. We describe a computational model for one such collective behaviour, phototaxis, in colonies of the cyanobacterium Synechocystis that move in response to light. The model replicates experimental observations of the response of cyanobacterial colonies to varied light regimes, and predicts the complex colony morphologies that arise as a result. The results suggest that tracking the trajectories of individual cyanobacteria may provide a way of determining their mode of information integration. Our model allows us to address the emergent

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nature of this class of collective bacterial motion, linking individual cell response to the large scale dynamics of the colony.

Introduction

Cells respond to a variety of sensory inputs, including chemical and physical signals. An experimentally measurable example of such behaviour involves cell motility, where cells alter their motion in response to an external signal $[1]$ $[1]$. Bacteria provide a particularly convenient model to investigate taxis to many types of stimuli, including pH changes $[2]$ $[2]$, oxygen $[3]$ $[3]$, osmolarity [\[4](#page-16-0)] and magnetic fields [[5\]](#page-16-0). Chemotaxis, where cells swim up (or down) chemical gradients, is an extensively studied example of cell taxis, most notably in flagellated Escherichia coli. However, while the responses of individual cells to single inputs have been well characterized and modeled [\[6](#page-16-0)], the mechanisms through which cells collectively respond to more complex and spatially structured combinations of inputs remain open to investigation.

Cyanobacteria exhibit phototaxis, or motion in response to a light stimulus [\[7\]](#page-16-0). When colonies of the model cyanobacterium Synechocystis sp. PCC 6803 are exposed to red or green light emanating from a single source, individual cells first move toward the edge of the colony nearest to the light source. There, they aggregate before further extending towards the source through regular, dense finger-like projections [\[8](#page-16-0)]. Variations in light intensity and wavelength induce responses that range from slower moving colony fronts $[8]$ to negative phototaxis $[9]$ $[9]$ $[9]$. Phototactic cells such as Synechocystis respond directly to the relative position of the light source [[10](#page-16-0)] and not to a spatio-temporal concentration gradient, as in the case of chemotaxis.

Unlike the flagellae-driven motion of E. coli, Synechocystis exhibits "twitching" or "gliding" motility which is slower and has lower directional persistence [\[11\]](#page-16-0). This mode of motility is facilitated by type IV pili (T4P). These pili attach to the substrate and retract to move the cell forward [\[11\]](#page-16-0). This type of motility is often also associated with complex polysaccharides, or 'slime', extruded by these cells. The presence of slime reduces the friction that cells experience during motion [\[12\]](#page-16-0). The T4P also add another collective component to gliding motility, since cells can also use them to attach to each other $[11]$. Further, while E. coli provides an example of a single-cell response that can be studied at high resolution, cells in their natural environments are often found in dense aggregates and biofilms where interactions between cells are harder to probe, yet cannot be ignored.

The non-linear collective response arising from cell-cell communication, as in quorum sensing, provides an example of how interactions between cells drives qualitatively different behaviour [[13](#page-16-0)]. These types of collective behaviour are often hard to capture in single cell models. Further, both light quality and direction can fluctuate in the natural environment, but the effects of such variation are not currently well understood. Several studies have explored the effects of varied illumination schemes on colony morphology $[14-19]$ $[14-19]$ $[14-19]$. In one recent experiment [\[19\]](#page-17-0), colonies of Synechocystis receive light incident on them from two different directions. These studies found that fingers from the colonies emerged along a direction intermediate between the directions of the light sources.

This raises the question of whether this collective behaviour at the level of the entire colony is best interpreted as arising from individual cells attempting to move along an intermediate direction determined by the vector sum, or whether it could also plausibly arise from the averaged response of individual cells responding to a single, randomly chosen light source at each time. Identifying which of these two scenarios occurs would require experiments that probe the coupled dynamics of receptor activation and downstream signaling, with consequences for cell motility. Such relationships are hard to establish in practice, and it is thus worthwhile to explore alternative ways of discriminating between such scenarios, guided by modeling.

Here, we quantitatively analyse the different modes of individual cell behaviour and their resultant colony morphologies in the context of a model for the light-directed motion of cells in cyanobacterial colonies. Our perspective on such collective phenomena is motivated by models for active matter $[20, 21]$ $[20, 21]$ $[20, 21]$, which describe the collective behaviour of systems of selfpropelled units. Our earlier model [[22](#page-17-0)] incorporated motion at the level of single cells, cell-cell interactions mediated via T4P and the decrease in surface friction through the deposition of slime. That model is extended here to incorporate what is known about the response of cells to variations in light intensity and wavelength, including the possibility of negative phototaxis.

Our modeling framework addresses recent experiments involving the complex illumination of cyanobacterial colonies. We reproduce experimental results and demonstrate how our model can be generalized to novel situations involving several light sources, each with a different wavelength and intensity. The model makes predictions regarding the trajectories of individual bacteria in cyanobacterial colonies. Importantly, we find that colony morphology cannot be used to uniquely infer mechanisms through which individual cells integrate information from multiple light sources, since the large-scale morphology of the colony is independent of whether individual cells decide to move along the vector sum of the light they receive, or whether they make stochastic decisions to move towards one or the other of these inputs at each step. However, examining the trajectories of single cells within such colonies provides a way of distinguishing between different scenarios for information integration. Furthermore, we find that qualitatively similar results are obtained even when individual cells respond heterogeneously. This is largely a consequence of the fact that the motion of groups of cells that interact with each other involves a collective component.

Methods

The model used in this paper is adapted from a previously proposed model $[22]$ $[22]$ $[22]$ for the collective motion of cyanobacterial colonies illuminated by a single light source. This model described the behaviour of independently motile cells that can physically interact with each other, and move towards a distant light source. The three essential components of this model are: (i) the ability of cells to locate the position of a light source that biases their direction of motion; (ii) the forces that cells exert on other cells in their vicinity through T4P, and; (iii) the deposition of slime by individual cells, which reduces the friction that they encounter.

In this paper, we extend this earlier model to describe the response of an individual cell to variations in (i) light intensity (ii) wavelength, and (iii) the number and orientations of different light sources. Our current model describes two scenarios for how cells might integrate directional input in the form of separated light sources to which they respond. We use LED as a representation for a generic light source in all our figures. The schematic of $Fig 1(a)$ describes the general setup of our simulations involving cell colonies subjected to two light sources, whose individual intensities and wavelengths may vary. While these modifications were central to being able to describe the experiments in [\[19\]](#page-17-0), they are also crucial for a more accurate representation of a broader set of experiments, as well as ecological contexts. We briefly describe this model below.

Modeling complex illumination

We consider arrangements of individual colonies that receive light from sources placed at different locations. The light from each source may also present a different wavelength. The intensity arising from each light source is assumed to be uniform within a colony but can vary

across colonies. The angle that the line joining the colony centre to a light source k makes with the horizontal is given by Θ_k , as illustrated in the schematic of Fig 1(b) . For ease of description, we label the directions as (North, South, East, West), or (N, S, E, W) as shown in Fig 1(b). In all cases, each light source is placed one unit away from the grid that defines the colony locations. The probability that cells within a given colony attempt to move towards light source k , in the Θ_k direction is captured by $p_k.$ The schematic of $\underline{\mathrm{Fig}\ 1(\mathrm{b})}$ shows two light sources separated by an arbitrary angle, leading to an inhomogeneous distribution of intensities across the colony.

We replicate the experimental setup of $[19]$ $[19]$ $[19]$ as closely as possible, as illustrated in Fig $1(b)$. In these experiments, the intensity of light experienced by a colony varies with its distance from the source. We assume that p_k for each light source varies inversely with the distance, d_k , between the center of the colony and the light source.

The cell

Each cell is modeled as a disc of radius R, specified by a two dimensional vector, $X_i = (x_i, y_i)$. As in $[22]$, when colonies are subjected to a single light source k , individual cells attempt to move in the direction Θ_k with probability p_k or in a random direction in the interval [0, 2 π] with probability $1 - p_k$.

We extend this model to include illumination from multiple light sources. Fig 2 displays two possible ways in which individual cell movement in such colonies may be biased towards

two distinct light sources, placed to the North and to the East of a colony. The first column (Fig 2(a) and 2(b)) illustrates the case where the sources are switched on individually, while the second column (Fig $2(c)$ and $2(d)$) illustrates two distinct cell responses in the case where both light sources are switched on, viz. stochastic switching and vector integration.

Stochastic switching. At each time step, cells may decide to move in the direction Θ_k of any of the light sources k with probability p_k , or in a random direction in the interval $[0,2\pi]$ with probability $1 - \sum p_k$. This is illustrated in Fig 2(c).

Vector integration. The vector joining the centre of each colony at $t = 0$ with light source k is represented by $v_k = p_k(\cos\Theta_k, \sin\Theta_k)$. Individual cells attempt to move along the vector sum of these light sources, $v_{\text{vec}} = p_{\text{vec}}(\cos\Theta_{\text{vec}}, \sin\Theta_{\text{vec}}) = \sum v_k$. Thus, cells attempt to move in the direction Θ_{vec} with probability p_{vec} or in a random direction in the interval [0, 2 π] with probability $1 - p_{\text{vec}}$. This is illustrated in Fig 2(d).

In both mechanisms, each cell *i*, at time *t*, picks a direction, Θ_i^t as described above. The decision of the cell to move in a particular direction is modeled through a force

$$
\mathbf{G}_i^t = f_0(\cos \theta_i^t, \sin \theta_i^t),\tag{1}
$$

where we choose $f_0 = 1$ to set the scale of forces. The direction in which a given cell actually moves is determined both by this chosen direction as well as by the forces it experiences from other cells in its neighbourhood. These forces, arising from the interaction between cells, are described below.

Cell-cell interactions

Each cell is assumed to have a fixed number m of T4P. These can exert forces on randomly chosen cells that lie within a certain distance ℓ of its centre. During each time step, a cell j can exert a force $f_{ji} = K_{ji}(\cos\theta_{ji}, \sin\theta_{ji})$ on a randomly chosen neighbouring cell *i* where θ_{ji} is the angle that the vector from cell *i* to *j* makes with the horizontal. The magnitude K_{ii} of this force depends on the distance D_{ii} between the cells *i* and *j*:

$$
K_{ji} = (1 + k_1(\tanh(k_2(D_{ji} - 2R)) - 1))/m,
$$

We use a sigmoidal form for K_{ii} that is repulsive at short distances. This penalizes cell overlaps through a soft-core repulsion. In these simulations, we choose values of $k_1 = 1$ and $k_2 = 2$. As shown in [S4 Fig](#page-15-0) of the Supporting Information, the colony morphologies obtained for this choice of values is robust with respect to changes in k_1 and k_2 . Higher values of k_2 facilitates the emergence of fingers and this is more pronounced at larger k_1 . A detailed discussion of the motivation for choosing this specific form of K_{ij} , and of the associated parameter values, is pre-sented in [[22](#page-17-0)].

The cell i thus experiences a total external force,

$$
\mathbf{F}_i = \sum_j f_{ji} \tag{2}
$$

from other cells j in its neighbourhood. The net force acting on this cell at each time step t is then $\mathbf{G}_i^t + \mathbf{F}_i^t$.

Slime deposition

The slime deposited by cells is assumed to be deposited on a regular square lattice underlying the colony. Each grid point is specified by (r, c) . Cells are assumed to deposit slime at every time step. The amount of slime, S^t at time t associated with the grid point closest to each cell's centre, is incremented by an amount S_{rate} in each time step.

$$
S^{t+1}(r,c) = S^t(r,c) + S^{rate},
$$
\n(3)

We further assume that once the amount of slime at a grid point exceeds S_{max} , no more slime is added to that point. Additionally, we assume that slime does not decay or diffuse once deposited.

Cell movement

The motility of a cell depends on the amount of slime at the grid point closest to the cell centre. The positions of cells are updated in parallel, as in standard agent-based models, with parameters chosen such that the maximum distance that a cell in a slime-rich background can move in a single time step is a tenth of the cell radius. In slime-poor backgrounds, the reduced

mobility of the cell implies that it moves a smaller distance in the same time. At the end of each time step, the position of each cell is updated through the following scheme:

$$
\mathbf{X}_{i}^{t+1} = \mathbf{X}_{i}^{t} + (\mathbf{G}_{i}^{t} + \mathbf{F}_{i}^{t}) / \gamma_{i}^{t},
$$
\n
$$
\tag{4}
$$

where $\gamma_i^t = \gamma_0 S_0 / S^t(r,c)$ is a friction factor that is associated with the presence of slime lying below a cell, where S_0 is the initial slime concentration within the colony and γ_0 is the friction encountered by cells within the colony at $t = 0$.

Simulation details

We simulate cyanobacterial colonies containing $\mathcal{N} = 500$ cells that are initially distributed randomly over a circular spatial domain representing a colony. We have verified that the results are qualitatively invariant for larger system sizes (see Supplementary Information [S1](#page-14-0) and S_2 Figs for results obtained for $\mathcal{N} = 500$, 2000 and 5000 over a range of values of p_{photo}). In experiments on phototaxis a colony is typically of the order of tens of thousands of cells. For example, in [\[19\]](#page-17-0) each colony, which is around 2.5mm in diameter, consists of \sim 33000 cells, which is less than one order of magnitude higher than the maximum number of cells considered in our simulations. As shown in Supplementary Information [S3 Fig](#page-15-0), colonies with the same ρ have similar colony morphologies over a range of $\mathcal N$. The parameter of significance here is the density ρ which, in experiments, is roughly 0.06 as calculated from the methods described in [\[19\]](#page-17-0) and is close to the value $\rho = 0.1$ used in these simulations.

Unless otherwise indicated the parameters used in our simulations are listed in Table 1. Synechocystis cells are around $1\mu m$ [[7\]](#page-16-0) in radius, and we use this to define our cell radius R, which is also assumed to be the basic length scale in our model. Each cell in our model can have up to *m* appendages, and in these simulations, we use $m = 4$ [[23\]](#page-17-0). The maximum length *l* of an appendage is taken to be four cell lengths $[24]$ $[24]$ $[24]$. For a detailed discussion of the cell force parameters (k_1,k_2), see [[22](#page-17-0)]. Cells can move at a maximum of 0.1 body lengths per unit time [\[11\]](#page-16-0). To our knowledge there has not been a detailed investigation of slime deposition rate and how this affects cell speed. For a more detailed discussion of the system parameters see [\[22\]](#page-17-0).

At the start of each simulation, cells are distributed uniformly over a circular colony, where the initial slime concentration is the same for all grid points within the colony. At each time step for each cell we determine \mathbf{G}_i^t from $\underline{\mathrm{Eq}}$ (1). For each cell we also determine which of its neighbours it is attached to. Using this information, we can calculate the external force experienced by each cell \mathbf{F}_i^t from $\underline{\text{Eq}}(2)$. We then update the positions of each cell using the equation of motion (4) , which involves the net force $(\mathbf{F}_i^t + \mathbf{G}_i^t)$ and slime underlying the cell. Finally, we update the slime matrix $S^t(r, c)$ using $\underline{\mathrm{Eq}}$ (3).

Parameter	Quantity	Value	
N	number of cells	500	
R	cell radius		
ρ	cell density in colony	0.1	
l	appendage length	4R	
m	number of appendages per cell	4	
γ_0	inverse of initial cell speed	1/(0.1R)	
(k_1, k_2)	force parameters	(1, 2)	
$S_{\rm rate}$	slime deposition rate	0.1	
$p_{\rm photo}$	phototaxis probability	(0, 0.05]	
.			

Table 1. Parameters used in simulations (unless mentioned otherwise).

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Fig 3. Cell colonies in a linear grid under complex illumination. Morphologies of several colonies under illumination from a single light source placed at the East. Each experiences a different intensity of incident light, depending on its location. The placement of the light source is such that the easternmost colony experiences the greatest incident light intensity. Thus, p_{photo} decreases linearly towards the West, as shown in the bottom bar. Each colony contains $\mathcal{N}=500$ cells, and the model was simulated for 4 \times 10⁴ time steps.

Results

Colony morphologies at varying light intensities

We consider colonies of cells that exhibit positive phototaxis. These are placed in a simple onedimensional array consisting of 5 colonies, an arrangement similar to that used in the experiments of [\[19\]](#page-17-0), and which is illuminated from the East. These experiments tested the response of colonies to varying intensities of red light. In our simulations, this variation in intensity is described by a single parameter, p_{photo} , which varies across colonies.

Fig 3 describes how the colony morphology changes as p_{photo} is varied between 0.05 and 0.01, simulating the drop in intensity as one moves from East to West across the arrangement of colonies. Initially, due to the absence of slime outside the colony, cells are unable to cross the colony boundary despite being phototactic and motile. This leads to a temporary aggregation of cells at the initial colony boundary and an associated build up of slime, prior to the formation of fingers. At smaller p_{photo} , the colony emits small, slightly distorted fingers oriented towards the light source. The emerging fingers appear to meander more at low p_{photo} and the velocity of fingers in the direction of the source is reduced. As p_{photo} is increased, fingers become longer and more prominent. In addition, their velocity in the direction of the source is increased. The time-evolution of fingers at different p_{photo} values is illustrated in Supplementary [S1 Movie.](#page-15-0)

Our results, shown in $Fig 3$, recapitulate the following experimental observations: (i) there is a light-flux dependent increase in the movement bias of cells in colonies, and (ii) finger sizes decrease at lower illumination.

Colony morphologies under multiple light sources

We generalize the linear complex illumination described in the previous section by simulating intensity variation along two directions, an arrangement that was also considered in the experiments of $[19]$ $[19]$ $[19]$. In these experiments, colonies were arranged on a grid and exposed to two sources of red light, placed North and West of this grid.

In Figs 4 and 5 , we consider a set of 25 colonies placed in a 5 \times 5 array and illuminated by two light sources. The intensities decrease along E-W and N-S directions as one moves away from each light source. The rules by which individual cells respond to this complex illumination can be either through Stochastic switching ($Fig 4$) or Vector integration ($Fig 5$) mechanisms, as described below.

[Fig 4. C](#page-7-0)ell colonies in a square grid under complex illumination in the stochastic switching case. Configurations of a number of cell colonies, arranged in a square grid, illuminated by two different light sources placed at N and E. This arrangement of light sources creates a gradient in intensity. Cells stochastically switch between biasing their motion towards one of the two light sources, with the effective intensity of the light sources towards N and E represented by p_1 and p_2 respectively. The map of p_1 and p_2 across a 5 × 5 grid is represented in (a) and (b) respectively. The morphology of colonies placed on this 5 \times 5 grid is shown in (c). Each colony contains $\mathcal{N} =$ 500 cells, and the model was simulated for 4×10^4 time steps.

Stochastic switching. The intensity of the light from the North and East experienced by a colony is captured by p_1 and p_2 respectively, using the convention of [Fig 1\(b\).](#page-3-0) Fig 4(a) and 4(b) show the variation of light intensity (as expressed in terms of p_1 and p_2) over the colony array. Within each colony the p_1 and p_2 are constant. Cells sense these separate light sources and, at each time step, make a stochastic decision to move towards either light source, weighted by these probabilities. Each cell can thus decide to move towards North and East with probability p_1 and p_2 respectively, or can move in a random direction, chosen uniformly from [0, 2 π], with probability $1 - p_1 - p_2$.

As expected, and as shown in $Fig 4(c)$, colonies extend more pronounced fingers towards the closer light source. Colonies that are equidistant from each source extend fingers in the general N-E direction but appear to meander more. Note that the colony at the N-E corner of the grid extends fingers towards the S-W because the light sources are South and West of it.

Vector integration. As in the case of stochastic switching, the intensity of the light experienced by a colony from the North and East is captured by the probabilities p_1 and p_2 respectively. Fig $5(a)$ shows this map of probabilities p_{vec} experienced by each colony, where p_{vec}

[Fig 5. C](#page-7-0)ell colonies in a square grid under complex illumination in the vector integration case. Configurations of a number of cell colonies, arranged in a square grid, illuminated by two different light sources placed at N and E. This arrangement of light sources creates a gradient in intensity. Cells bias their motion towards the vector sum of the two light sources. (a) shows the effective total intensity of the light sources in the direction of the vector sum (p_{vec}) is represented across a 5 \times 5 grid. The direction of the vector sum of the light sources at each of the grid points is shown in (b) The morphology of colonies placed on this 5×5 grid is shown in (c). Each colony contains $\mathcal{N} = 500$ cells, and the model was simulated for 4×10^4 time steps.

arises from the vector sum of p_1 and p_2 . <u>Fig 5(b)</u> shows the direction θ_{vec} of the vector sum. Within each colony the p_{vec} and θ_{vec} are constant. At each time step, cells make a decision to move in the direction of θ_{vec} , with a probability of p_{vec} and can move in a random direction, chosen uniformly from [0, 2 π] with probability 1 – p_{vec} . As seen in Fig 5(c), the qualitative nature of all colony morphologies are very similar to those for the stochastically switching case. The qualitative dependence of finger properties on intensity remain the same as in the one-dimensional case (see [Fig 3\)](#page-7-0).

Comparing these two cases, we note that while the decision making process of individual cells is different, the final colony morphologies are strikingly similar. We reason as follows: although individual cells may decide to move according to one rule or the other, the overall morphology of the colony is a collective property arising also from the dynamic interaction between moving cells. This similarity suggests that observations of gross colony morphology may not suffice to disentangle the underlying mechanism of phototaxis at the single cell level.

To understand how individual cells integrate information in scenarios where they are exposed to complex illumination, we consider the information that can be extracted from individual cell trajectories.

Distinguishing stochastic switching and vector integration scenarios

We considered a series of arrangements of light sources in order to systematically investigate the behaviour of cell trajectories under the different scenarios of stochastic switching and vector integration. We study a colony in which cells experience light from two sources that are placed on a circle centered at the colony. This ensures that the cells experience the same intensity of light, regardless of the angle that the light source makes with the East-West axis.

We consider three cases, where a pair of light sources are placed 30˚, 60˚ or 90˚ North/ South of East, respectively. In each case, we track the trajectories of individual cells over time, computing the angles that the trajectory makes, over each unit time interval, with the horizontal. In Fig 6, we visualize the distribution of these angles as rose plots, where the height of each bar represents the relative probability that cells move in that angle.

Fig $6(a)$ – $6(c)$ represents the stochastic switching case, where at each step cells stochastically bias their motion in the direction of one of the light sources. Fig $6(d)$ –6(f) shows results for the vector integration case, where at each step cells bias their motion in direction of the vector

Fig 6. Rose plots of the angle of motion for stochastic switching and vector integration cases. Distribution of angles of motion of cells in colonies exposed to a pair of light sources placed at different positions relative to it. The probabilities are represented by the histogram of the angles made by the movement of a cell in a single time step. The light sources are placed at angles 30˚ (a,d), 60˚ (b,e) and 90 $^{\circ}$ (c,f) North/South of East as shown in the respective figures. The intensity (and related p_{photo}) is constant across all figures and is also assumed not to vary significantly across the size of the colony. In (a-c) at each step cells stochastically bias their motion in the direction of one of the light sources. In (d-f) at each step cells bias their motion towards the vector sum of the light sources. In all cases, the intensity of color of the bars of the rose plots are related to their magnitude. In each subfigure, the insets show the final colony morphology. Each colony contains $N = 500$ cells, and the model was simulated for 4×10^4 time steps for the case $p_1 = p_2 = 0.05$.

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sum of the light sources. We have verified that qualitatively identical results can be obtained even at larger system sizes as shown for $\mathcal{N} = 5000$ in [S5 Fig](#page-15-0) of the Supporting Information.

In the case where the cells stochastically switch between detecting the two light sources, we find that the rose plots are characterized by two clear peaks in the directions of the light sources. This is in clear contrast to the corresponding rose plots obtained for the vector integration case, where cell motion is biased in the direction of the vector sum of the direction of the two light sources.

As the angle between the two sources is increased in the vector integration scenario, the cancellation of the effects due to the two opposing sources becomes more prominent. In contrast, the rose plots in the stochastic switching scenario indicate a clear bias in the direction of each individual light source. This difference between the two scenarios is particularly prominent in the case where the light sources are placed 90˚ North/South of East. Here, we observe two peaks that point in opposite directions for the stochastic switching case, while for the vector integration case we find that the distribution of angles in the rose plots is nearly uniform.

Response of colonies with mixtures of cell types sensitive to different wavelengths

Cell colonies can be heterogeneous, expressing different levels and types of light receptors. The collective response in such communities can thus be influenced by the relative proportions of cells that respond differently to complex illumination.

In [Fig 7,](#page-12-0) we show results from our simulations for colonies consisting of varying proportions of cells that are sensitive to either red or green light. The simulated colonies are subjected to red and green light sources placed at different angles from the East-West axis. The ratios green-light sensitive cells to red-light sensitive cells are varied across 50:50, 25:75 and 10:90. Since each cell detects only one light source, the distinction between stochastic switching and vector-integration scenarios is inapplicable.

We start from an initial configuration where cells sensitive to different wavelengths are seeded at random. As the proportion of cells sensitive to red light is increased, the fingers are directed more towards the red light source. However, green-sensitive cells are also incorporated into these fingers as a result of cell-cell attachments. The green-light-sensitive cells in these fingers are not located at random, but tend to be found closer to the green light source. Finally, colonies consisting of roughly equal proportions of green and red-light sensing cells, tend to have more irregular fingers, an effect that is more prominent at intermediate angles between the two sources.

Negative phototaxis

Finally, we study the response of cell colonies to light sources that induce a negative phototactic response in cells. Experimentally, illuminating colonies directionally under UV light has been shown to lead to the formation of fingers extending in a direction opposite to the light source [[9\]](#page-16-0). We simulate a negative phototactic response through a probability that cells in the colony attempt to move away from the light source k, in the direction $\Theta_k - 180^\circ$, with the probability p_{photo} . As before, there is also a random component to the direction of motion and the attachments of cells dictate collective colony morphologies.

In [Fig 8](#page-13-0), we show results for negative phototaxis in initially circular cell colonies illuminated by UV light that is incident from the East. As in $Fig 3$, the length and rate of growth of fingers depends strongly on p_{photo} , with the difference that the fingers now extend away from the source rather than towards it.

[Fig 7. C](#page-11-0)olonies with mixtures of of cells sensitive to different wavelengths. Colonies are assumed to consist of two types of cells, each of which senses only one of the light sources. The cell types are indicated by green and red colors, corresponding to the wavelength of light they are sensitive to. The two different light sources, of the same intensity (and hence same p_{photo}), are placed at angles 30° (a, d, g), 60˚ (b, e, h) and 90˚ (c, f, i) North/South of East as shown in the respective figures. We consider the following proportions of cells that sense only red to those that sense only green: (a-c) 50:50 (d-f) 75:25 (g-i) 90:10. Each colony contains $\mathcal{N} = 500$ cells, and the model was simulated for 4×10^4 time steps for the case where $p_{\text{photo}} = 0.05$ for both the red and green sensitive cells.

Discussion

In this paper, we explored the consequences of complex illumination on the shapes of cyanobacterial colonies. We used a computational model whose fundamental unit was the single cell. We modeled each such cell as an agent whose movement was dictated by its own interactions with external light sources, as well as from its interactions with its neighbours. The motion of the agent was facilitated by the slime that it encountered when moving. The model

accounts explicitly for the forces exerted, and experienced, by each cell due to its neighbours through attachments mediated via T4P.

In most experiments [[8,](#page-16-0) [18,](#page-17-0) [25\]](#page-17-0), the tip of the growing fingers consist of a tightly packed group of cells that move at a relatively constant speed once they leave colony. This is a feature of the fingers that emerge from the colony in our simulations as as well, and as shown in Fig. 3 of [[22](#page-17-0)], this speed is relatively constant. In our simulations, we see that the value of certain quantities, such as the dimensionless ratio of finger width to finger separation is ~ 1 . Various experimental images of colony morphology, including Fig. $2(A)$ from [[25](#page-17-0)] suggests that this ratio is in reasonable agreement with our results. In addition other gross measures such as time scales are in agreement with experimentally observed values, as can be seen from the following argument: The velocity of an cyanobacterial cell is known to be of the order of 0.1μm/s [\[11\]](#page-16-0). In our model, a cell in a slime-rich environment moves at speed $0.1R/\Delta t$, where the radius of the cell R is of the order of $1\mu m$ and Δt is the simulation time step. Matching this with the experimentally obtained value gives us $\Delta t = 1$ second. This is a reasonable value, as we observe finger formation over the course of $t \sim 10^5$ time units in our model which is \sim 27 hours, a value that is comparable with experiments $(1 - 2 \text{ days})$. A detailed quantitative comparison will lead to a more refined and informed model and to this end, we look forward to future experimental collaborations that can be used to calibrate our model.

We studied the morphologies of colonies under different light regimes to determine the mechanisms through which single cells integrate information from external cues, translating these into decisions regarding their motion. We investigated at least two major mechanisms by which phototactic cells could respond to light incident on them from different sources. The first was a stochastic switching scenario in which cells chose, at each time step, either to move towards a randomly chosen light source with a fixed probability, or to move in an arbitrarily chosen direction. In the second model, cells responded through what we term "vector integration", in which individual cells either chose to move along the vector sum of individual light sources, or chose, at each time step, to move in a random direction. The specific scenario applicable could also, in principle, depend on the wavelengths of light as well as the magnitude of the intensity that the cell is exposed to. We asked if the subtle difference between these scenarios, clearly distinct at the single cell level, could be inferred from large-scale measurements on colonies.

We observed that similar-looking colony morphologies could be obtained under two very different underlying mechanisms of single-cell response to complex illumination. To explore this further, we examined the statistics of the trajectories of individual cells within the colony. We concluded that extracting statistical features of individual cell trajectories could provide a way of distinguishing between these, and potentially other, mechanisms of single-cell response, even if the overall colony morphologies did not. We describe ways in which the relevant information can be extracted from ensembles of single cell trajectories.

At a more general level, colonies of phototactic bacteria provide a unique opportunity to test models of collective response in living systems. While individual bacteria can sense and move towards light [[10](#page-16-0)], the nature of colony morphologies is a function of the mechanical attachments between cells, mediated by their T4P $[26]$ $[26]$, as well as of the slime that cells lay down [\[27\]](#page-17-0).

Slime, in particular, plays a unique role. It allows for density-dependent motility [\[28\]](#page-17-0), reminiscent of quorum-sensing mediated by small molecules in bacteria. Unlike quorum-sensing, however, slime-mediated interactions between cells can be time-dependent, since the motion of bacteria at later times can be influenced by slime laid down by other bacteria at an earlier time. In conventional quorum-sensing, driven by the production and detection of small diffusible autoinducers [\[29\]](#page-17-0), the relatively large diffusion constant of small molecules implies that the time delays between production and detection can be safely ignored.

Swimming bacteria such as E. coli interact via a practically instantaneous and long-ranged hydrodynamic interaction mediated by the fluid [\[30,](#page-17-0) [31](#page-17-0)]. This is a feature of virtually all biophysical models for the interactions between swimming bacteria. In contrast, the interactions between cyanobacteria are short-ranged, involve direct mechanical forces mediated by T4P, and could also be delayed in time. Thus, phototaxis differs in a number of qualitative ways from the much-studied problem of bacterial chemotaxis.

Computational models such as the one we describe here, once benchmarked, can be used to investigate behaviour that can be experimentally tested in order to identify regimes of the parameter space that are most likely to provide strong evidence for one hypothesis over another. Such models can also be used to study behaviour in other types of bacteria that interact with each other using T4P. The agent-based approach discussed here makes it easy to incorporate inter-cellular variations in response to stimuli, such as in colonies comprising mixtures of cells that respond only to a particular incident wavelength. These may also naturally correspond to the situation in heterogeneous ecological communities of phototactic bacteria, such as in hot springs [[32](#page-17-0)].

Additional detail can be incorporated into the model we describe here, allowing us to bridge the gap between single cell and collective response more effectively, as more data becomes available. Finally, there are fascinating, and as yet unanswered, questions that relate to how cells in bacterial colonies might localize pili and photoreceptors to activate downstream signaling pathways. Coupling such signaling responses to cell-cell interactions and cell motion would enable us to address a number of questions concerning the mechanobiology of collective cell behaviour.

Supporting information

[S1 Fig](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s001). Morphologies of colonies in a linear grid under structured illumination obtained for different values of N **. Colonies are illuminated by a single light source placed at the East.** Each experiences a different intensity of incident light, depending on its location relative to the light source, such that the easternmost colony experiences the greatest incident light intensity. Thus, p_{photo} decreases linearly towards the West, as shown in the bar below each row. The number of cells in each row is indicated by $\mathcal N$, and the model was simulated for 3 \times 10⁴ time steps. Note that in each of the panels we have used a slime matrix of dimension 400×400 , which is larger than those used for figures in the main text (300×300) . (TIFF)

[S2 Fig](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s002). Morphologies of colonies obtained for different values of N **. Morphologies of three** colonies, each under illumination from a single light source placed at the East. The number of cells in each colony is (left-right) $\mathcal{N} = 500$, $\mathcal{N} = 2000$ and $\mathcal{N} = 5000$ cells, as indicated below the corresponding panels. Each colony experiences a light intensity of $p_{\text{photo}} = 0.05$ and the model was simulated for 3×10^4 time steps. In each case, we display a close-up of the morphologies around the colony edge, where the dimensions of each box is identical. The displayed results indicate that the morphology of the fingers is relatively independent of the number of cells N .

(TIFF)

[S3 Fig](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s003). Morphologies of cell colonies of different values of N **and densities** ρ **. Morphologies** of several colonies under illumination from a single light source placed at the East. Each colony experiences a light intensity of $p_{\text{photo}} = 0.05$, the number of cells in each panel is indicated by ${\cal N}$, the colony density is indicated by ρ and the model was simulated for 3 \times 10⁴ time steps. Note that in each of the panels we have used a slime matrix of dimension 500×500 , which is larger than those used for figures in the main text (300×300) . (TIFF)

[S4 Fig](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s004). Effect of changing the parameters k_1 **and** k_2 **. Snapshots of the colonies at** $t = 5 \times 10^4$ for different values of the parameters k_1 and k_2 in a system of size $\mathcal{N}=5000$ for the situation where a light source is placed at infinity (to the right of the colony). The panel highlighted by the red box shows results obtained using $k_1 = 1$ and $k_2 = 2$, which are the values used in the manuscript.

(TIFF)

[S5 Fig](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s005). Rose plots of the angle of motion for stochastic switching and vector integration cases for $\mathcal{N} = 5000$. Distribution of angles of motion of cells in colonies exposed to a pair of light sources placed at different positions relative to it. The probabilities are represented by the histogram of the angles made by the movement of a cell in a single time step. The light sources are placed at angles 30˚ (a,d), 60˚ (b,e) and 90˚ (c,f) North/South of East as shown in the respective figures. In (a-c) at each step cells stochastically bias their motion in the direction of one of the light sources. In (d-f) at each step cells bias their motion towards the vector sum of the light sources. In all cases, the intensity of color of the bars of the rose plots are related to their magnitude. Each colony contains $\mathcal{N} = 5000$ cells, and the model was simulated for 3×10^4 time steps for the case $p_1 = p_2 = 0.05$. (TIFF)

[S1 Movie.](http://journals.plos.org/ploscompbiol/article/asset?unique&id=info:doi/10.1371/journal.pcbi.1007807.s006) Time lapse movie showing the positions of cells and the slime they lay down over the course of a simulation. We start with an array of colonies under a single light source placed to the East of the colonies as described in Fig. 3. Here p_{photo} decreases linearly towards the West, as shown in the bottom bar. Each subsequent frame is separated by 500 time steps. Each colony contains $N = 500$ cells, and the model was simulated for 4×10^4 time steps. (GIF)

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